

$$\bar{\Pi} = \frac{1}{2} \sum_e \{u\}^T \cdot [K] \cdot \{u\} - \{u\}^T \cdot \{F\}$$

FEM SOFTWARE AND SERVICES

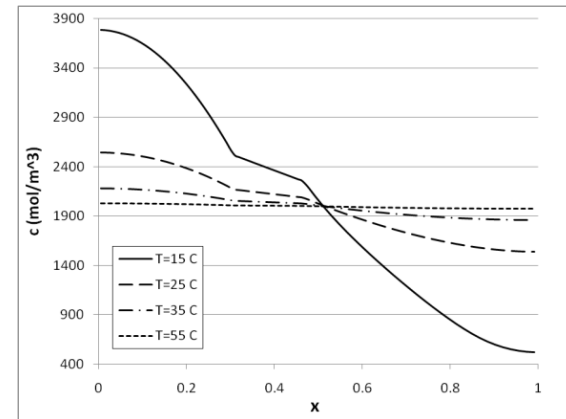
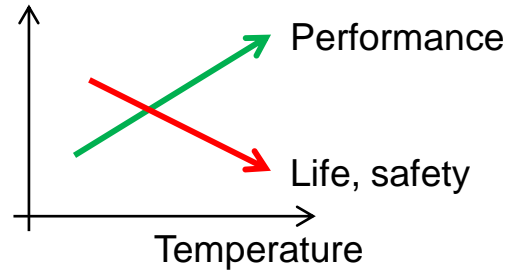


# Efficient lithium-ion battery pack electro-thermal simulation

Lucas Kostetzer, M. Eng

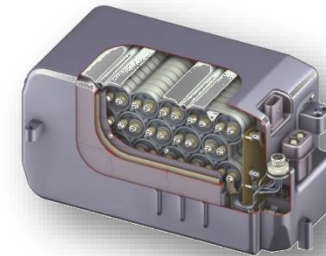
# Introduction

- Li-ion batteries are temperature sensitive



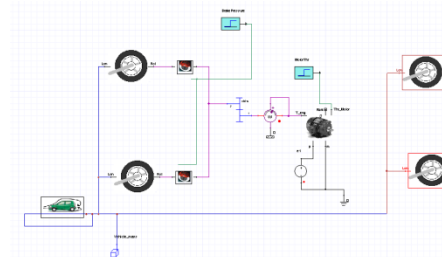
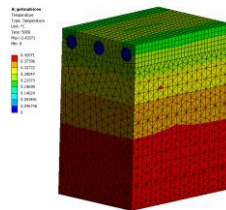
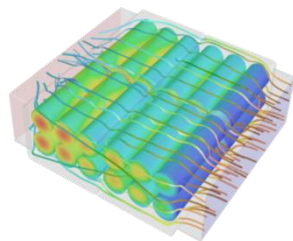
- Battery pack needs active cooling/heating

- Efficient energy usage
- Control systems



- Reduce the prototype efforts:

- Simulation aided design**



# Outline

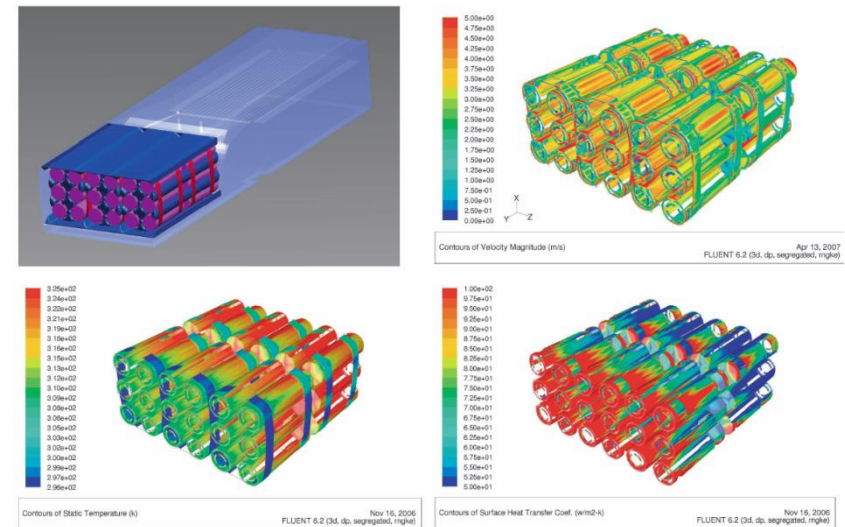
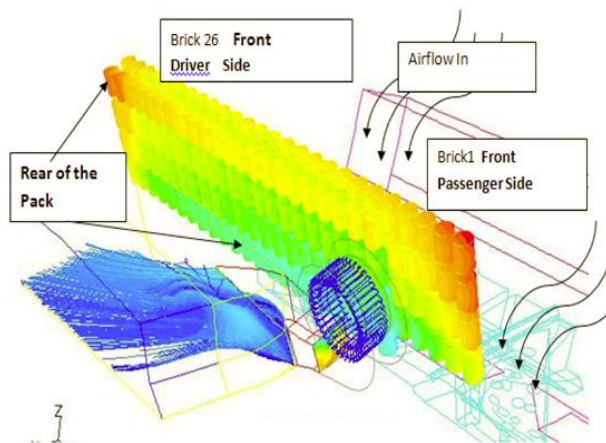
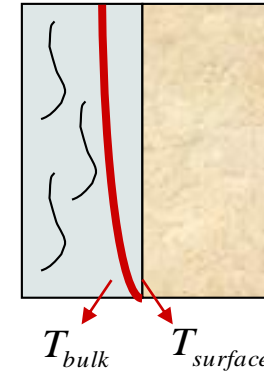
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- Traditional thermal modeling approach
- Efficient simulation with Model Order Reduction
- Electro-thermal battery pack simulation
- Summary

# Thermal simulation

- Heat transfer phenomena
  - Heat conduction,
  - Radiation
  - Convection (fluid flow)
  
- CFD/FEM
  - Standard tool for Industry

boundary layer



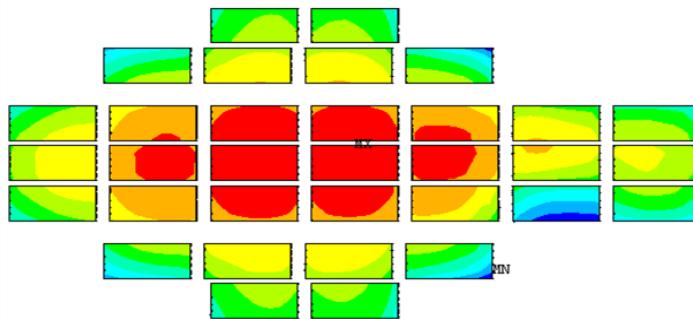
1. D. Ghosh, P. D. Maguire, and D. X. Zhu, " Design and CFD Simulation of a Battery Module for a Hybrid Electric Vehicle Battery Pack," SAE 2009-01-1386  
 2. D. Ghosh, K. King, B. Schwemmin, D. Zhu, "Full Hybrid Electrical Vehicle Battery Pack System Design, CFD Simulation and Testing," SAE 2010-01-1080

Drage, P., Kussmann, C., Jagsch, S., " Simulating Thermal Management of Battery Modules for Propulsion of Hybrid Vehicles. EAAC 2007

# Battery Thermal Management > Simulation challenge

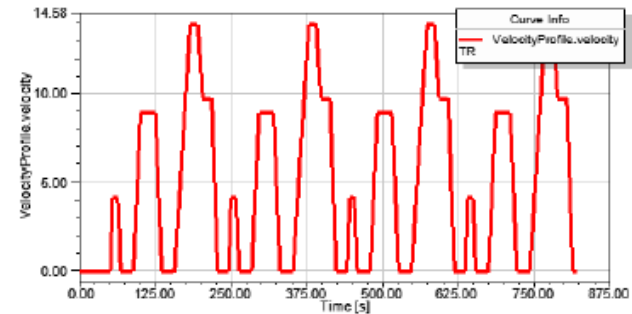
## ■ FEM transient CPU costs

- 5 min per time step (1000k nodes) (intel i7, 4 cores)
- ~1000 time steps = 80hrs!



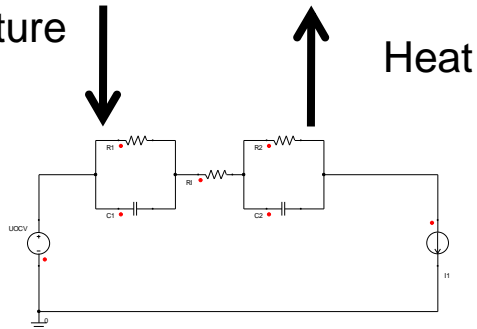
+

## Dynamic loads



+

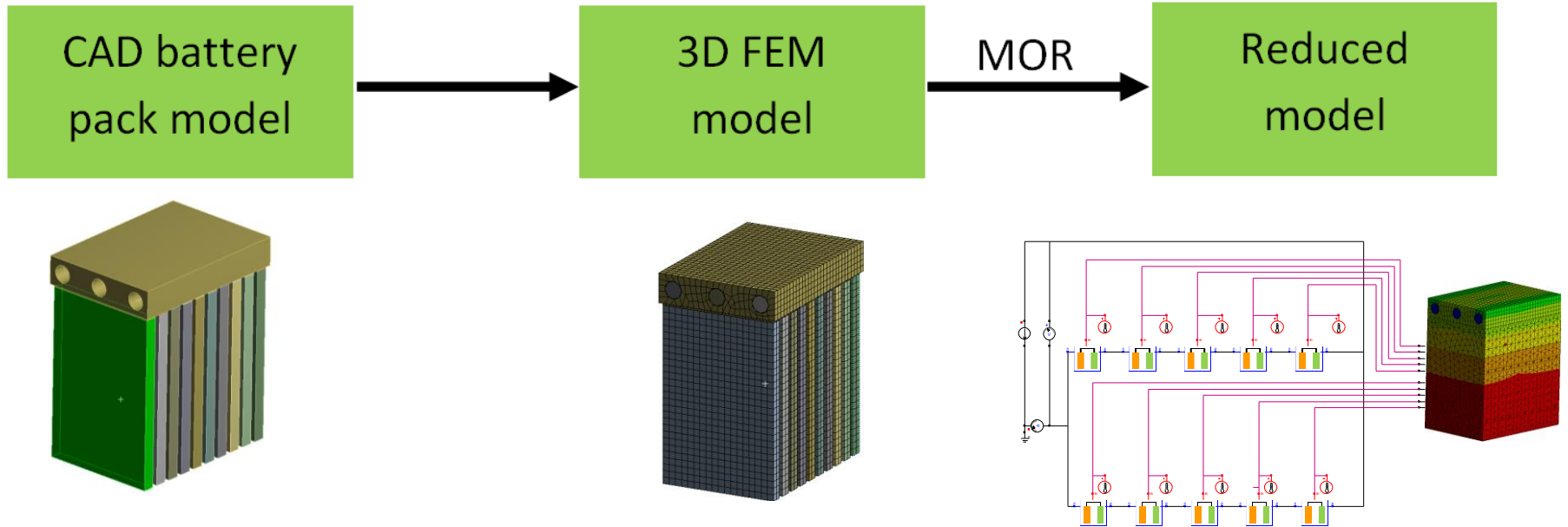
Temperature



Controller  
Vehicle model  
...

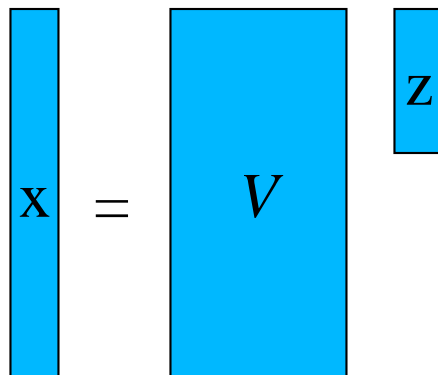
**Low CPU cost is needed > Reduced order thermal model**

# Bring 3D thermal model to system level



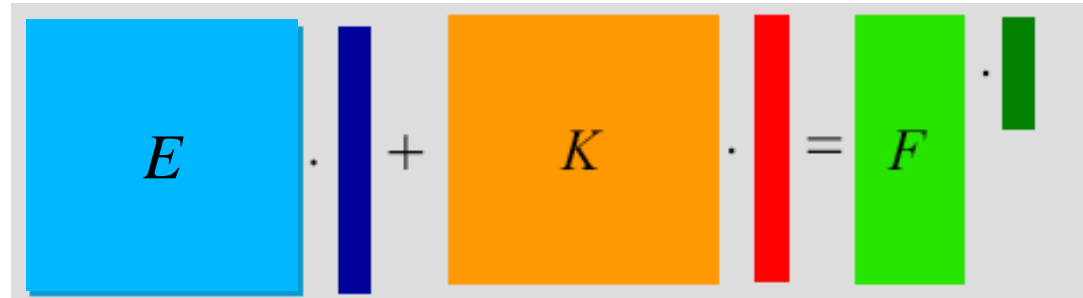
# MOR for ANSYS: <http://ModelReduction.com>

- Projection onto low-dimensional subspace

$$\mathbf{x} = V\mathbf{z} + \boldsymbol{\varepsilon}$$


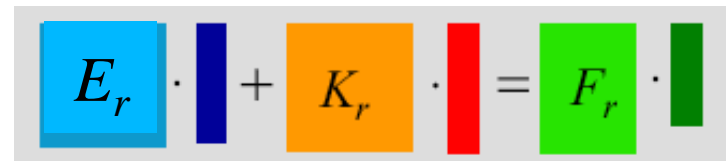
The diagram illustrates the projection of a vector  $\mathbf{x}$  onto a subspace defined by the matrix  $V$ . The vector  $\mathbf{x}$  is represented by a blue vertical bar on the left. The matrix  $V$  is a larger blue rectangle in the center. The resulting vector  $\mathbf{z}$  is a smaller blue vertical bar on the right. The equation  $\mathbf{x} = V\mathbf{z} + \boldsymbol{\varepsilon}$  is written above the diagram.

$$E\dot{\mathbf{x}} + K\mathbf{x} = B\mathbf{u}$$



The diagram shows the full finite element model equation  $E\dot{\mathbf{x}} + K\mathbf{x} = B\mathbf{u}$ . It consists of a blue square matrix  $E$ , a blue vertical vector, a plus sign, an orange square matrix  $K$ , a red vertical vector, an equals sign, a green square matrix  $F$ , and a green vertical vector.

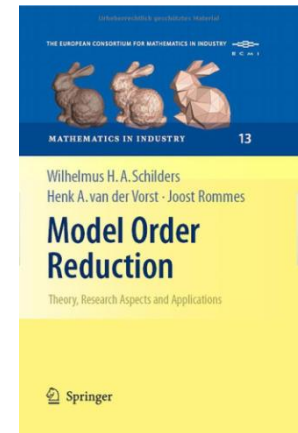
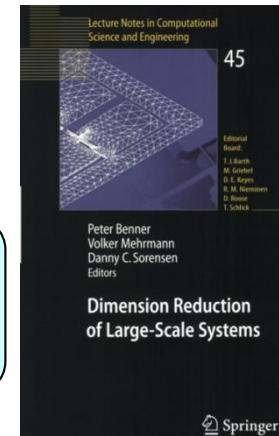
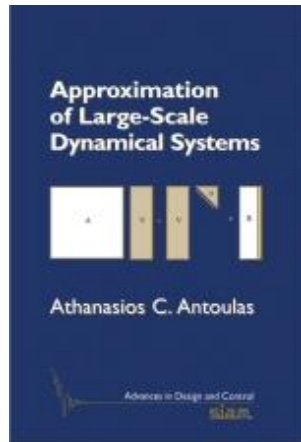
$$V^T E V \dot{\mathbf{z}} + V^T K V \mathbf{z} = V^T B \mathbf{u}$$



The diagram shows the reduced finite element model equation  $E_r \dot{\mathbf{z}} + K_r \mathbf{z} = F_r \mathbf{u}$ . It consists of a smaller blue square matrix  $E_r$ , a blue vertical vector, a plus sign, a smaller orange square matrix  $K_r$ , a red vertical vector, an equals sign, a smaller green square matrix  $F_r$ , and a green vertical vector.

- Advantage:
  - NO transient solution with the original FEM model is necessary
  - Highly accurate (linear systems)
  - As accurate as the original FEM model

# MOR in Modern Mathematics



Linear Dynamic System, ODEs

Control Theory  
BTA, HNA, SPA  
 $O(N^3)$

Moment Matching via Krylov subspaces.  
Iterative, based on matrix vector product.

Low-rank Grammian,  
SVD-Krylov

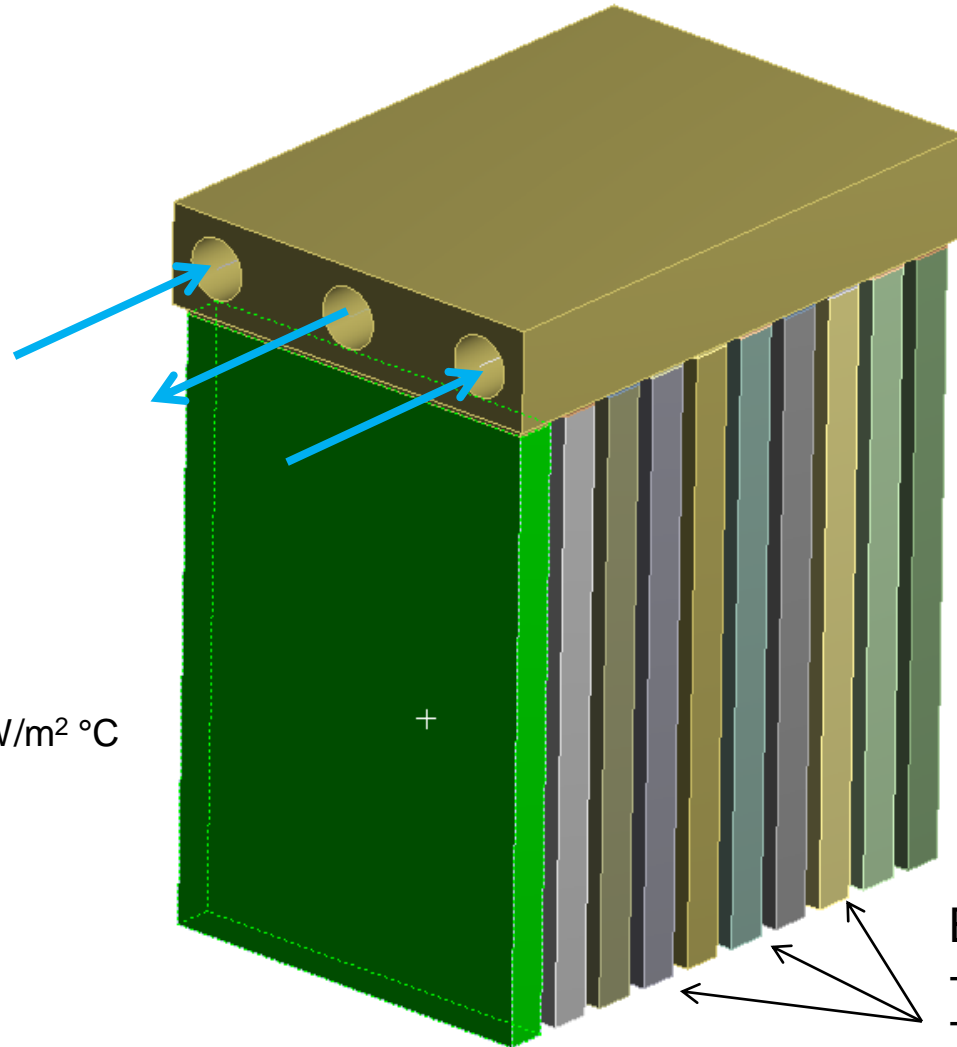
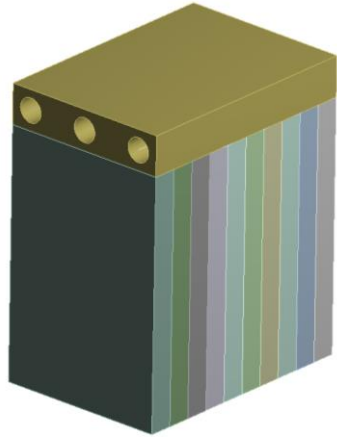
one-side Arnoldi process

double-side Lancsoz algorithm

MOR for ANSYS



# Battery pack FE thermal model in ANSYS WB



## Cooling channels:

- FLUID116
- Mass flow: 0.1 kg/s (water)
- Heat transfer coefficient:  $500\text{W/m}^2\text{ }^\circ\text{C}$
- Inlet Temperature:  $20^\circ\text{C}$

- Battery Cells
- 10 cells
- Orthotropic heat conductivity

# FEM analysis

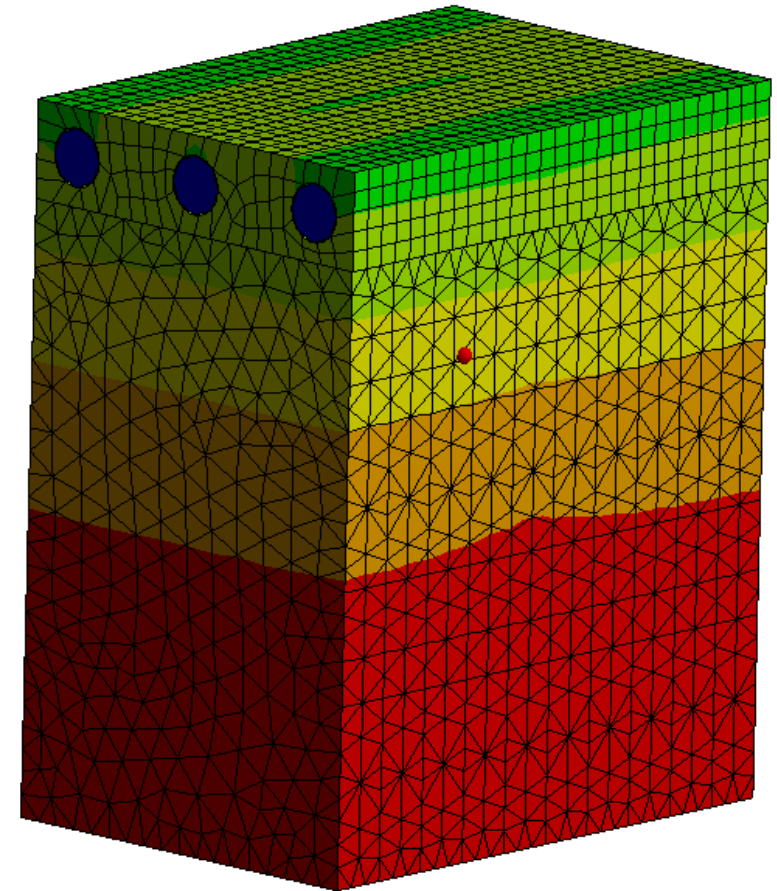
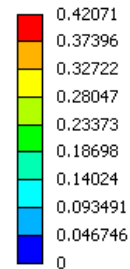
## ■ What one can get?

- Field of
  - Temperature
  - Heat flux
- Total heat fluxes...

## ■ CPU costs

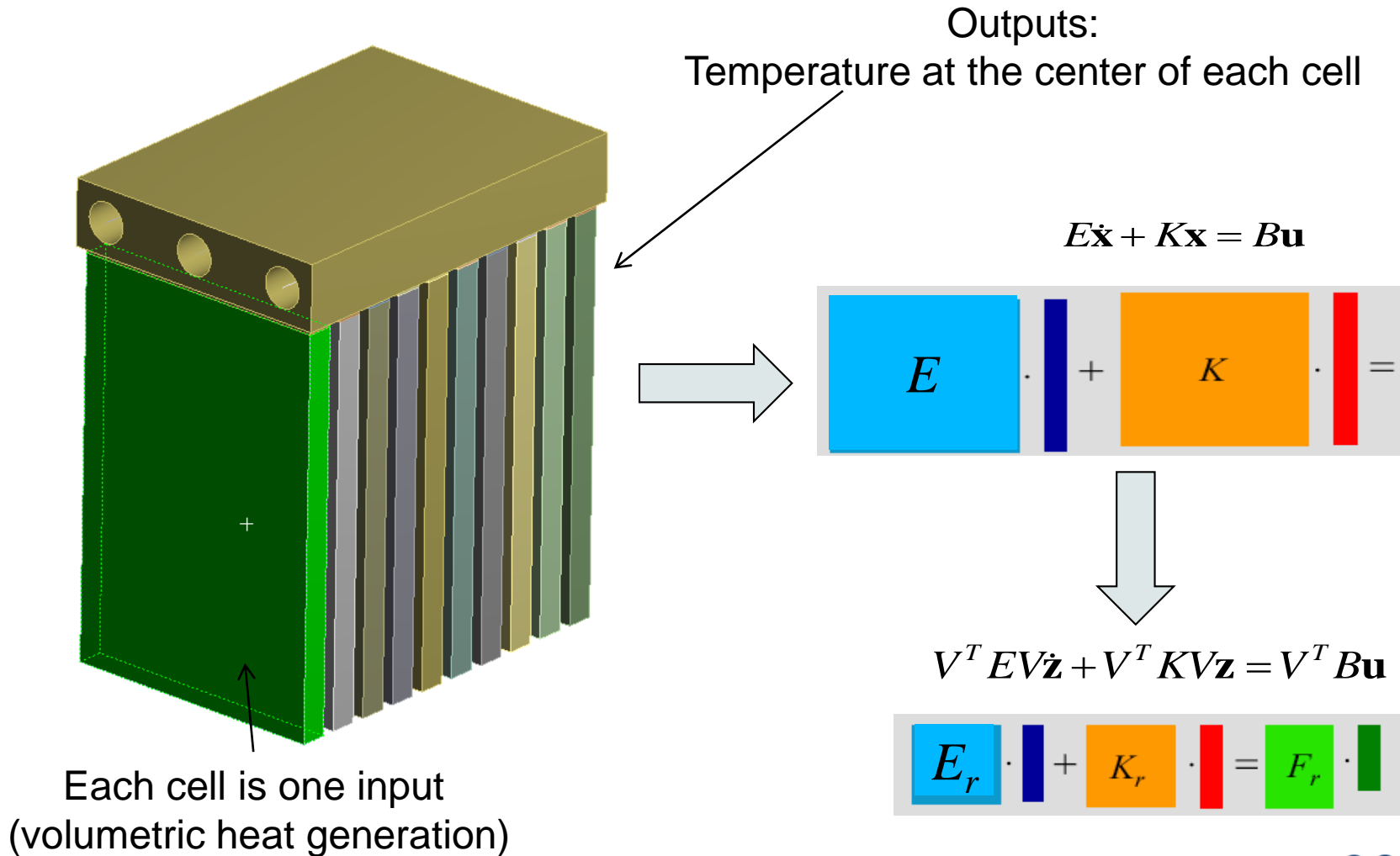
- Mesh: 150k nodes
- CPU cost per time/load step : ~31s

**A: getmatrices**  
Temperature  
Type: Temperature  
Unit: °C  
Time: 5000  
Max: 0.42071  
Min: 0



# MOR - preparation

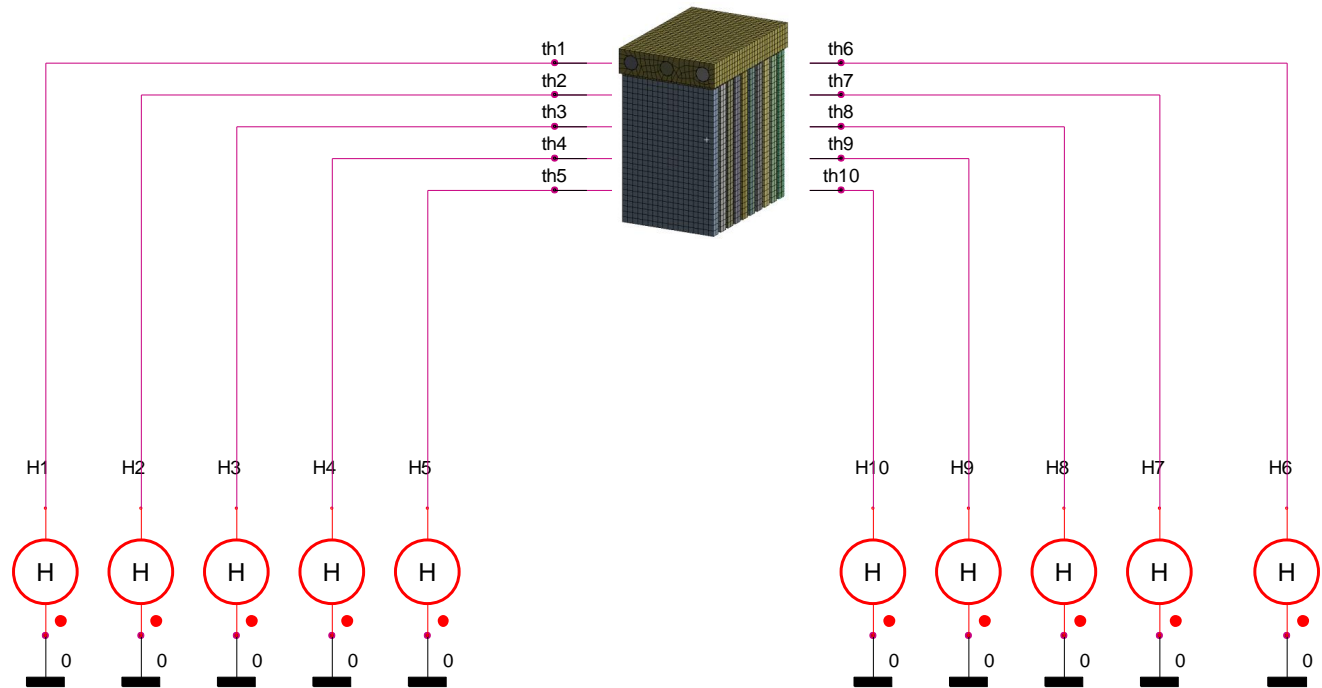
- Terminal concept (IN/OUT)



# Battery reduced order model

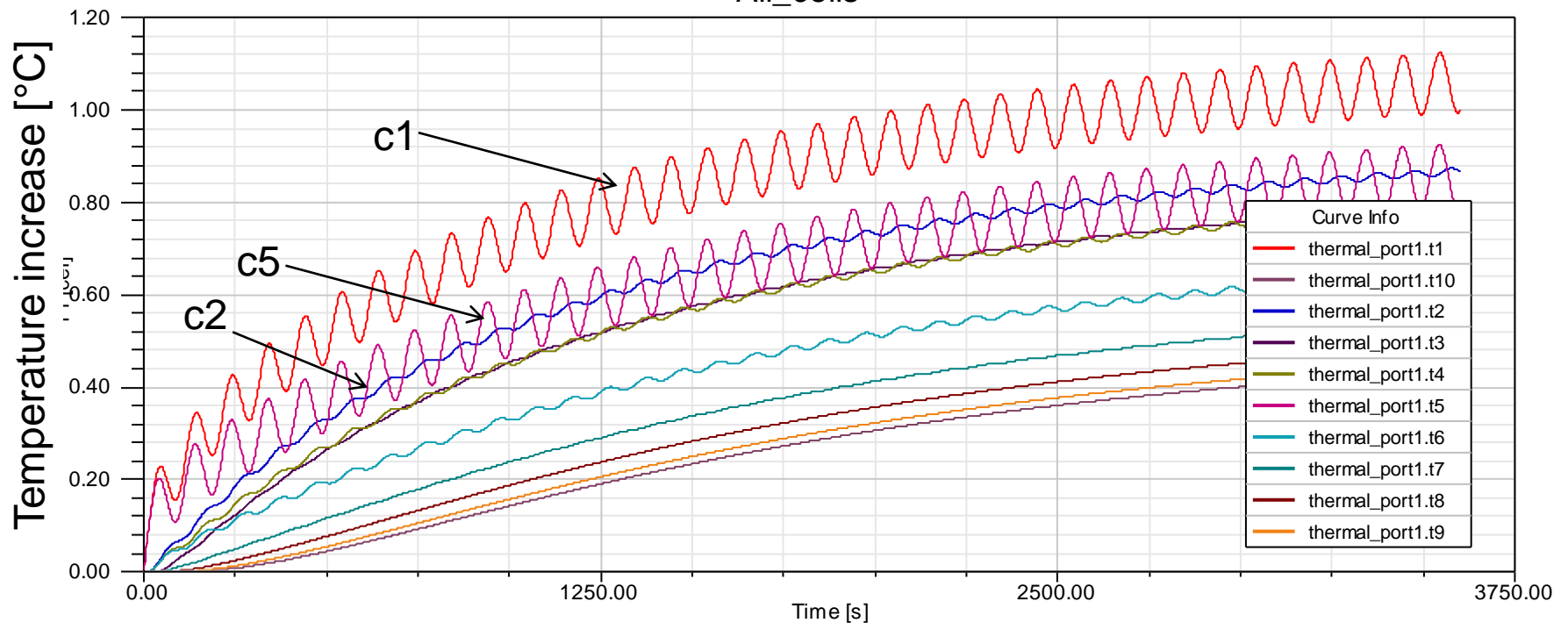
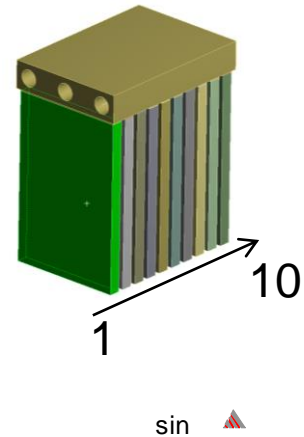
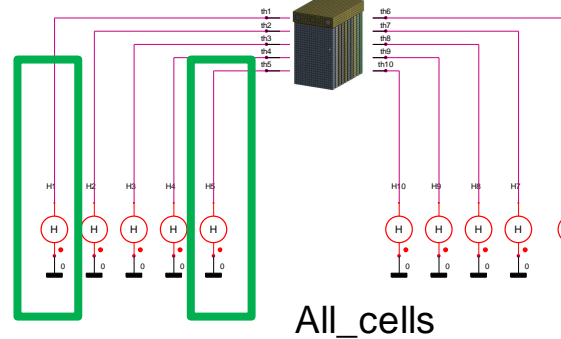
## ■ ROM

- 10 inputs /outputs
- Dimension : 100 (from original 150.000)
- Solved in ANSYS Simplorer

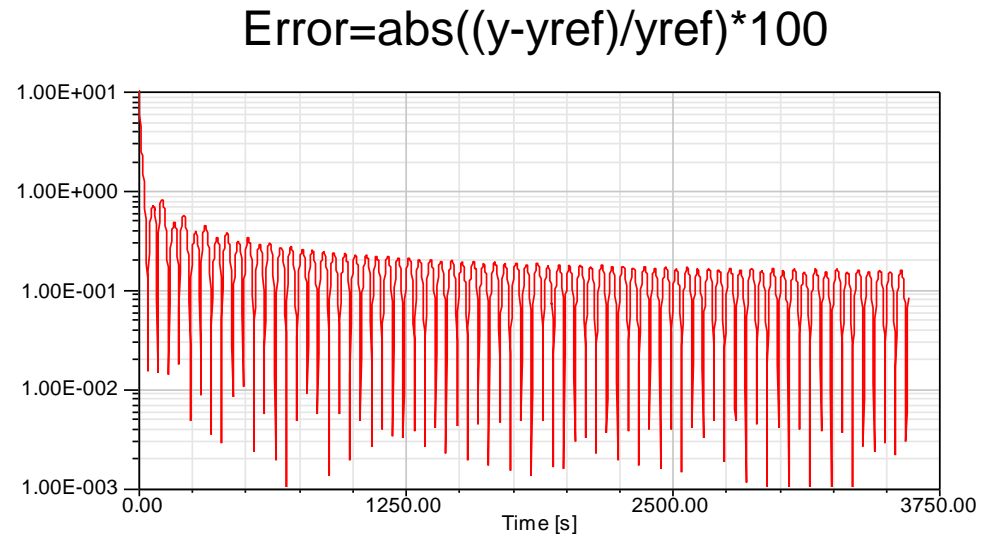
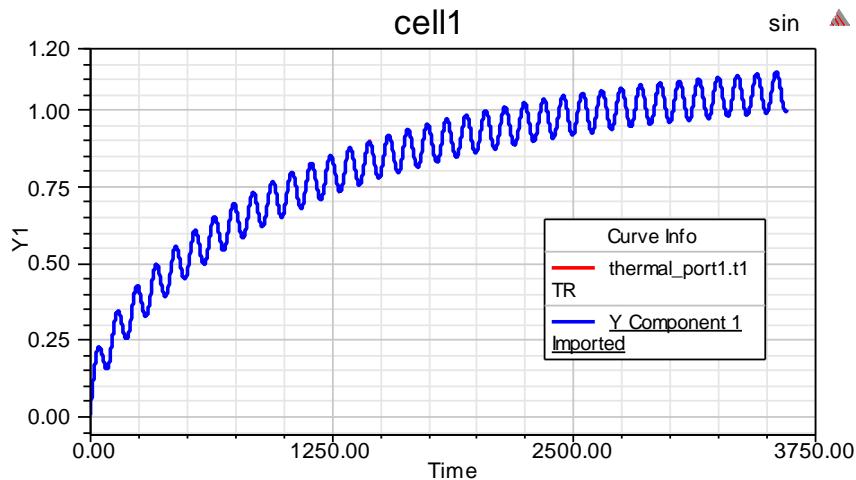


# Verification case

- Sinusoidal power for cells 1 and 5,  $f=0.01\text{Hz}$ , 20W max power



# Verification case – ROM vs Full (ANSYS)



Fixed time step: 1s, Total time: 3600s

Full (ANSYS) CPU time: 47750s (13.2hrs)

ROM CPU time: **35.9s**

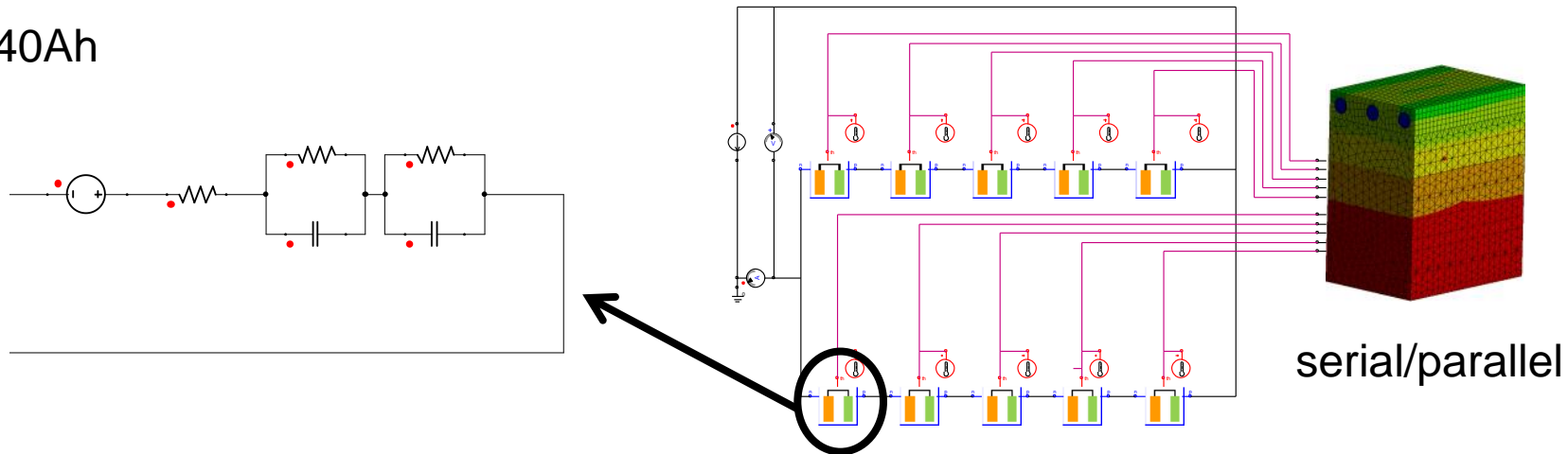
Speedup solution factor: 1300x faster

Error smaller than 2%

# Electro-thermal battery pack model

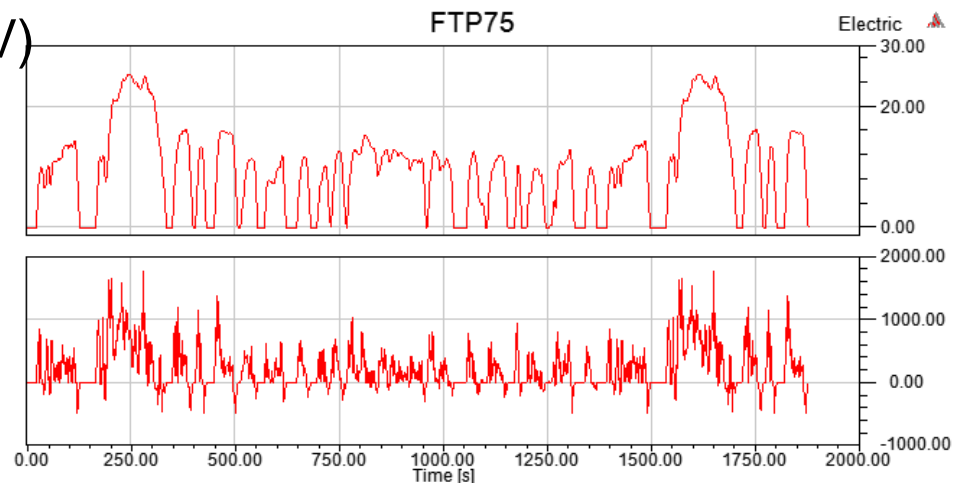
- Circuit based electrical model

- 40Ah



- Vehicle Power Train Model (EV)

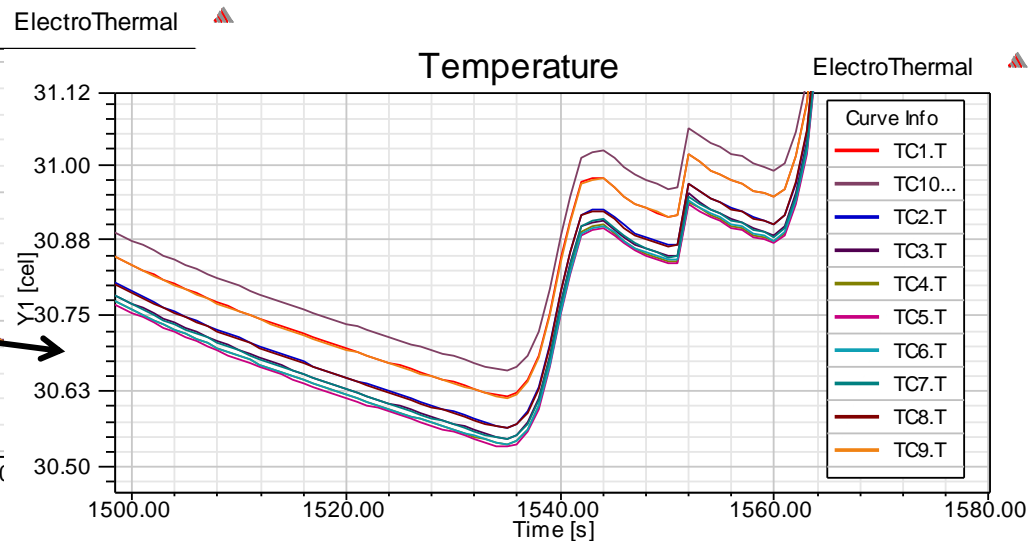
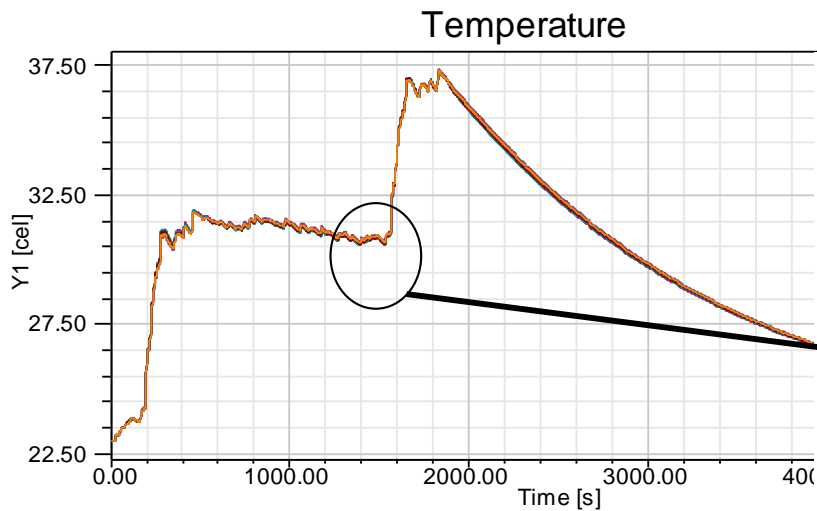
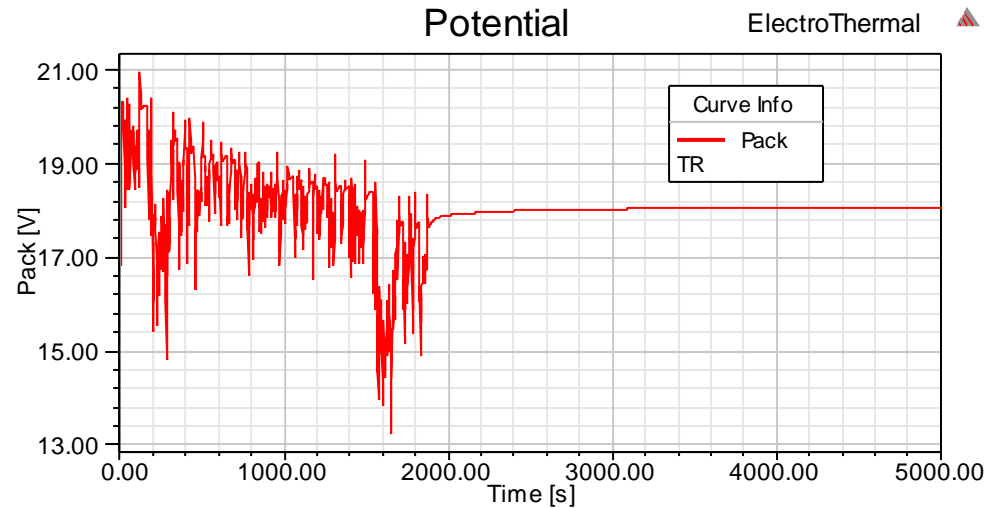
- 1150 kg, 42kW motor
- Drive train model
  - FTP75 drive cycle



# Results over EV onver FTP 75 drive cycle

## ■ Simulation

- Physical time: 5000s
  - $t < 1800s$  (FTP75)
  - Cooling phase
- CPU time: 166s

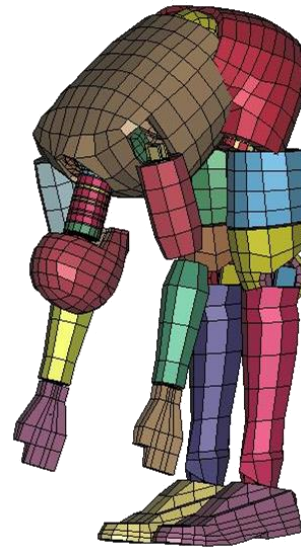




# Summary

- Projection via Krilov subspaces are efficient and accurate
  - Differences of full (FEM) vs ROM are under 2%
  - Speedup of 1300x
- Battery pack thermal responses in complete drive cycles are simulated in a minute scale
  - >Control design and complete simulation
- Method for accurate electro-thermal system level design
  - IGBT's, MEMS, Sensors, ....

Thank you for your attention



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